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# Abnormal grain growth in ultrafine grained Ni under high-cycle loading 

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#### Abstract

Abnormal grain growth can occur in polycrystalline materials with only a fraction of grains growing drastically to consume other grains. Here we report abnormal grain growth in ultrafine grained metal in a rarely explored high-cycle loading regime at ambient temperature. Abnormal grain growth is observed in electroplated Ni microbeams with average initial grain sizes less than 640 nm under a large number of loading cycles (up to $10^{9}$ ) with low strain amplitudes ( $<0.3 \%$ ). Such abnormal grain growth occurs predominantly in the family of grains whose $<100>$ orientation is along the tensile/compressive loading direction. Micromechanics analysis suggests that the elastic anisotropy of grains dictates the thermodynamic driving force of abnormal grain growth, such that the lowest strain energy density of the $<100>$ oriented grain family dominates grain growth. This work unveils a unique type of abnormal grain growth that may be harnessed to tailor grain microstructures in materials.


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Most technologically important materials are polycrystalline and thus consist of a number of grains separated by grain boundaries (GBs). Grain growth via GB migration is a ubiquitous phenomenon in polycrystalline materials under high thermomechanical loads $[1,2]$. If grains grow uniformly over the entire sample, it is called "normal grain growth". On the contrary, when grain growth occurs inhomogeneously, i.e., with only a fraction of grains growing drastically to consume other grains, it is called "abnormal grain growth". Grain sizes and their spatial distribution can strongly influence the physical and chemical properties of materials [3]. Abnormal grain growth can exacerbate degradation and lead to premature failure of materials [4]. Interestingly, abnormal grain growth has been recently harnessed to grow large-area single-crystalline metals that can be further used as substrates to grow large-area single-crystalline two-dimensional materials like graphene for applications in macroelectronics [5]. Hence, understanding grain growth is essential to control grain microstructures for achieving the desired properties of materials.

While both normal and abnormal grain growth have been studied in the past [6-16], here we report the unexpected abnormal grain growth of ultrafine grained (UFG) Ni in a rarely explored

[^0]high-cycle loading regime, which involves a large number of cycles (up to $10^{9}$ ) with low strain amplitudes ( $<0.3 \%$ ), at ambient temperature. We employ a unique MEMS microresonator-based setup to generate high-cycle bending loads on Ni microbeams, such that the largest cyclic tension/compression along the beam's length direction is generated in the beam surface layers where abnormal grain growth is observed. Our micromechanics analysis suggests that the elastic anisotropy of single-crystalline grains in polycrystalline aggregates plays a critical role in the observed abnormal grain growth, albeit with low driving forces of grain growth. The occurrence of such kind of abnormal grain growth is facilitated by the high number of load cycles (up to $10^{9}$ ) for achieving a pronounced cumulative effect of grain growth. Hence, this unusual grain growth response stands in stark contrast to other previously observed grain growth behaviors under large plastic strains and/or high temperatures [6-16], including those studies under cyclic loading [4,17-27]. Our results suggest a mechanism map of grain growth as illustrated in Fig. 1, whereby such kind of abnormal grain growth occurs in a special loading regime of temperature $T$ and maximum strain $\varepsilon_{\max }$ applied (highlighted in blue), giving low driving forces of grain growth.

We observed abnormal grain growth in UFG Ni microbeams with a face-centered cubic (fcc) crystal structure under the highcycle bending load excerted via a MEMS microresonator, at a testing frequency of 8 kHz [28-30]. The microresonator shown in


Fig. 1. Schematic mechanism map of grain growth in the space of temperature ( $T$ ) and maximum strain $\left(\varepsilon_{\max }\right)$ applied to polycrystalline materials. At relatively low $T$ (around room temperature $T_{\text {room }}$ ) and $\varepsilon_{\max }$ (around $0.2 \%$ ) grain growth is driven mainly by a need to release elastic energy and thus dictated by elastic anisotropy of single-crystalline grains. The capillary effects of GB energy and surface energy play an increasing role in driving grain growth with increasing $T$. In contrast, when $\varepsilon_{\max }$ is large, grain growth is driven mainly by large plastic dissipation.

Fig. 2a was fabricated with the MetalMUMPs process from MEMSCAP, which employed a LIGA technique to fabricate an electroplated Ni microbeam of $20 \mu \mathrm{~m}$ thick. Electroplating was performed using a conventional additive-free sulphamate bath at $30^{\circ} \mathrm{C}, \mathrm{pH}=4$, with a direct current (DC) density of $20 \mathrm{~mA} / \mathrm{cm}^{2}$. As a result, a strong [001] fiber texture in the out-of-plane ( $Z$ ) direction (marked in Fig. 2a) is formed with large columnar grains [3134]. This is confirmed by the EBSD grain orientation maps in the out-of-plane ( Z ) and beam's length ( X ) directions of an untested microbeam, which was obtained from a horizontal cut halfway through the Ni layer thickness (at $Z=10 \mu \mathrm{~m}$ ), see Fig. 2b and c. As shown in the ion beam image of the Ni layer sidewall (see Fig. 2a), the bottom $2.5 \mu \mathrm{~m}$ layer has a microstructure of ultrafine equiaxed grains. Fig. 2d and e show the EBSD maps of an untested microbeam from a horizontal cut at $Z=2.5 \mu \mathrm{~m}$ from the bottom of the Ni layer, indicating a [001] fiber texture in the surface normal direction (also shown with the inverse pole figure (IPF) plots in Fig. 2f). The area-weighted average grain size is less than 640 nm for $Z<2.5 \mu \mathrm{~m}$, and is $\sim 2 \mu \mathrm{~m}$ in the columnar part of the microbeam (i.e., the top $17.5 \mu \mathrm{~m}$ ). Using electrostatic actuation $[28,29]$, the microbeam can be driven at resonance ( $\sim 8 \mathrm{kHz}$ ), resulting in its cyclic bending deformation. The amplitude of rotation is measured at the beginning of each fatigue test, with a precision of $\sim \pm 1 \mathrm{mrad}$, and the corresponding strain amplitude at the edges of the microbeam $\varepsilon_{\mathrm{a}}$ is determined with a precision of $0.01 \%$ [35]. We used these devices over the past decade to investigate the small-scale fatigue behavior of electroplated Ni [35-41]. The fatigue behavior of these microbeams is mainly dictated by the top $17.5 \mu \mathrm{~m}$, where the microstructure is columnar. The bottom $2.5 \mu \mathrm{~m}$ layer, with an equiaxed ultrafine grained microstructure, experiences the same loading as the rest of the microbeam. In the following, we show extensive abnormal grain growth occurring only in the bottom layer.

Abnormal growth of grains preferably along the [100] cyclic tensile/compressive direction (X-axis) is revealed by the band contrast images and the corresponding grain orientation maps in the X direction (IPF-X) for five fatigued specimens (Fig. 3). As noted earlier, these images and maps were taken from horizontal slices at $\sim 1 \mu \mathrm{~m}$ from the bottom of the microbeam. The right column of Fig. 3 lists the number of abnormally large grains (ALG), defined as a size of at least $1 \mu \mathrm{~m}$, which represents about twice the initial mean grain size (ranging from less than 300 nm at $Z=1 \mu \mathrm{~m}$ to

640 nm at $Z=2.5 \mu \mathrm{~m}$, due to the gradient in grain size along the Z axis at the bottom of the microbeam; see Fig 2a). Fig. 3a shows a specimen tested at $\varepsilon_{\mathrm{a}}=0.31 \%$ for $1.2 \times 10^{7}$ cycles. Significant abnormal grain growth at such a low $\varepsilon_{\mathrm{a}}$ has occurred along the edges of the microbeam, i.e., at the location experiencing the largest amplitude of cyclic tensile/compressive strains in a bent beam. No grain growth occurred within a distance of $\sim 1.5 \mu \mathrm{~m}$ from the neutral axis located at the center of the microbeam (marked by the yellow dashed line in Fig. 3a). Most of the large grains that resulted from deformation-induced grain growth have an elongated shape along the $X$ direction, with a maximum size of $\sim 3 \mu \mathrm{~m}$ in the Y direction. This result indicates that the local strain at a position $3 \mu \mathrm{~m}$ from the edges is not large enough to induce grain growth; the corresponding local strain is estimated approximately as $0.15 \%$ for a microbeam width of $12 \mu \mathrm{~m}$ in the Y direction. Some grains become longer than $10 \mu \mathrm{~m}$ in the X direction, suggesting substantial GB migration under the applied cyclic strain. It is important to note that as shown in the grain orientation map in Fig. 3a, most of the large grains have a near [100] orientation in the X direction. This is evidently the result of preferential growth of grains of the [100] orientation by consuming grains of other orientations in the X direction.

Fig. 3b presents a specimen tested at $\varepsilon_{\mathrm{a}}=0.18 \%$ for $1.3 \times 10^{8}$ cycles. Similarly, significant abnormal grain growth occurred as well, with elongated shapes along the $X$ direction and a [100] preferential orientation in the X direction. The main difference with Fig. 3a is that the largest grains grew in the Y direction much closer to the neutral axis, despite having a lower $\varepsilon_{\text {a }}$ ( 0.18 vs. $0.31 \%$ ). This is likely the result of fatigue cracks, which accelerate grain growth after a larger number of applied cycles ( $1.3 \times 10^{8}$ vs. $1.2 \times 10^{7}$ ) by locally raising the deformation and providing additional driving force, as shown in other studies [42,43]. Hence, the presence of fatigue cracks can be responsible for the irregular shape of the larger grains in the Y direction (compared to Fig. 3a). The large grains also exhibit a preferential orientation of [100] in the X direction.

Similar to Fig. 3a, Fig. 3c shows a specimen tested at the same strain level of $\varepsilon_{\mathrm{a}}=0.3 \%$, but for a total number of $6.0 \times 10^{7} \mathrm{cy}-$ cles. This specimen has many large grains with elongated shapes, as long as $10 \mu \mathrm{~m}$ in size in the X direction and $3-4 \mu \mathrm{~m}$ in the Y direction. This specimen has a fatigue crack that initiated from the side of the microbeam. Significant grain coarsening occurred in the fatigue-cracked region, with grains spanning the entire half-width of the microbeam. The large grains also exhibit a preferential orientation of [100] in the $X$ direction.

Fig. 3d presents a specimen tested at $\varepsilon_{\mathrm{a}}=0.25 \%$ for $2.4 \times 10^{5}$ cycles, i.e., at least 50 times less cycling (compared to Fig. 3a-c) for similar $\varepsilon_{\mathrm{a}}$. This sample presents nine ALGs, almost all of which have a [100] preferential orientation in the X direction. However, these ALGs are smaller than those in Fig. 3a-c and none of them have an elongated shape in the X direction. Hence, a significant amount of grain coarsening for the specimens showed in Fig. 3a-c likely occurred between $10^{5}$ and $10^{8}$ cycles, suggesting a continuous growth process for grains with a preferential orientation of [100] in the $X$ direction. The specimen shown in Fig. 3e ( $\varepsilon_{a}=0.15 \%$ for $1.0 \times 10^{9}$ cycles) does not show any grain growth. Hence, there appears to be a threshold of $\varepsilon_{\mathrm{a}}$, between 0.15 and $0.18 \%$ (grain growth was observed at $0.18 \%$; see Fig. 3b), below which no grain growth occurs, despite applying up to $10^{9}$ cycles.

Fig. 4 presents in more detail the orientation of ALGs for selected specimens. The left column highlights all the grains with less than $10^{\circ}$ misorientation from [100] in the X direction, while the right column only shows the ALGs. Each color in these maps of the right column represents one ALG, and the same color is used in the IPF X plot to show its orientation along the X direction. Comparison of the two maps of the left and right columns


Fig. 2. UFG Ni microbeam under high-cycle loading via a MEMS microresonator. (a) (Left) Ni MEMS microresonator, with (middle) magnified SEM image of the Ni microbeam, and (right) ion beam image of the $20-\mu$ m-thick Ni layer sidewall showing location of the layer of interest, i.e., within $2.5 \mu \mathrm{~m}$ from the bottom of the microbeam, which contains an equiaxed UFG microstructure. (b) and (c) Grain orientation maps in the out-of-plane ( $Z$ ) direction and in the beam's length ( $X$ ) direction, respectively, from an untested microbeam after a horizontal FIB cut halfway through the Ni layer thickness ( $Z=10 \mu \mathrm{~m}$ ); (d) and (e) Grain orientation maps in the $Z$ and $X$ directions, respectively, from the same untested microbeam after a horizontal FIB cut at $\sim 2.5 \mu \mathrm{~m}$ from the bottom of the Ni layer ( $Z=2.5 \mu \mathrm{~m}$ ); (f) IPF plots in the X , Y , and Z direction for Ni at $\sim 2.5 \mu \mathrm{~m}$ from the bottom (each black dot represents a pixel from the grain orientation maps).
from Fig. 4b-e shows that most of the ALGs have a near [100] orientation along X -axis, especially the elongated grains along X axis. Therefore, these results clearly demonstrate the favorable growth of the [100] grain family along the loading direction. While the bottom portion of the microbeams have a limited number of grains, Fig. 4a shows that there are at least 15-20 grains along each sidewall (experiencing the largest amplitude of cyclic tensile/compressive strains) along the microbeam length. These 30-40 grains on the two sidewalls are the most likely candidates to become ALGs under cyclic loading, and are sufficient in numbers to provide repeatable results.

To understand the main finding of abnormal grain growth with a preferential orientation of [100] in the X direction, we developed a micromechanics model to determine the thermodynamic driving force of grain boundary migration as a function of grain orientation. According to Eshelby [44], the thermodynamic driving force of migration of defects and inhomogeneities can be derived using the elastic energy-momentum tensor. For GB migration in a linear elastic material, the thermodynamic driving force per unit GB area, denoted as $F$, is given by the jump of $P_{l j} m_{l} m_{j}$ normal to the GB plane,
$F=\Delta\left(P_{l j} m_{l} m_{j}\right)=\Delta W-t_{i} \lambda_{i}^{\top}$
where repeated indices imply summation. In Eq. (1), $m_{i}$ is the unit vector normal to the GB plane; $\Delta W$ is the jump of the local elastic strain energy density across the GB; $t_{i}$ is the continuous traction vector at the GB and given by $\sigma_{i j} m_{j}$, where $\sigma_{i j}$ is the stress tensor
on one side of the GB; and $\lambda_{i}^{\top}$ is the transformation strain vector across the GB. We emphasize that $\Delta W$ is proportional to the square of stress, while $t_{i} \lambda_{i}^{\top}$ is linearly proportional to stress. When $F$ is low, the GB velocity is linearly proportional to $F$. As a result, the effect of $t_{i} \lambda_{i}^{\top}$ on the average GB velocity becomes zero after a fully reversed load cycle, such that $\Delta W$ dictates the average GB velocity and accordingly the direction of GB migration.

We considered a representative spherical grain embedded in a polycrystal (Fig. 5a and b). To determine the stress and strain in this spherical grain, we used a micromechanics model that combines the classical Eshelby inclusion solution [45] and the selfconsistent solution of the effective elastic moduli of the polycrystal [46]. While individual grains are elastically anisotropic, the polycrystalline aggregate with a random distribution of grain orientations has the effective isotropic elastic moduli. According to the Eshelby inclusion solution [45], the stress, strain and strain energy density are all uniform in a spherical grain embedded in a homogenized polycrystal. When the polycrystal is subjected to an applied tensile stress $\sigma_{0}$, the uniform strain tensor in this grain is given by
$\varepsilon_{i j}=U_{i j k l} n_{k} n_{l} \sigma_{0}$
where $U_{i j k l}$ is the constrained compliance tensor derived in [46], and $n_{k}$ denotes the unit vector along the tensile loading direction. Supposing this grain belongs to the [hkl] family along the loading direction, we expressed $n_{k}$ as $\left(n_{1}, n_{2}, n_{3}\right)=(h, k, l) / \sqrt{h^{2}+k^{2}+l^{2}}$ in the local cubic basis. After algebraic operation of Eq. (2), we de-

Test Conditions
Band Contrast

(c)


Fig. 3. Abnormal growth of the grains with [100] orientation in the cyclic tensile/compressive loading ( X ) direction. (a-e) Band contrast images and grain orientation maps in the X direction of horizontal slices obtained at $\sim 1 \mu \mathrm{~m}$ from the bottom of the microbeam for five fatigued specimens. Fatigue-induced cracks are indicated by white arrows.


Fig. 4. Grain orientation maps (left column) showing grains whose misorientation from [100] along $X$ is within $10^{\circ}$, and grain orientation maps (right column) showing only the ALGs (each orientation represented by a color), along with their location in the IPF X plot, for an untested specimen (a) and four fatigued specimens (b)-(e).



 strain energy density in each grain family as a function of grain orientation index $3 \Gamma$ under an applied tensile stress of 640 MPa .
rived the uniform strain energy density $W$ in this grain as

$$
\begin{align*}
W & =\frac{1}{2} L_{i j k l} \varepsilon_{i j} \varepsilon_{k l}=\frac{\sigma_{0}^{2}}{2} L_{i j k l} U_{r s i j} n_{r} n_{s} U_{\text {pqkl }} n_{p} n_{q}  \tag{3}\\
& =\frac{\sigma_{0}^{0}}{2}\left[\frac{3 a_{\mathrm{WU}}+4 b_{\mathrm{WU}}}{3}-4\left(b_{\mathrm{LUU}}-c_{\mathrm{LUU}}\right) \Gamma\right]
\end{align*}
$$

where $a_{\mathrm{LUU}}, b_{\mathrm{LUU}}$ and $c_{\mathrm{LUU}}$ represent the components of the product of $L_{i j k l} U_{r s i j} U_{p q k l}$ by using the symbolic tensor notation defined in our previous publication [46]; and $\Gamma$ is the grain orientation index defined as
$\Gamma=\frac{h^{2} k^{2}+l^{2} k^{2}+h^{2} l^{2}}{\left(h^{2}+k^{2}+l^{2}\right)^{2}}$
varies between 0 and $1 / 3$ to cover all the grain families with random orientations, and it takes $0,1 / 4$ and $1 / 3$ for the representative grain families of [100], [110] and [111], respectively. Under an applied stress $\sigma_{0}=640 \mathrm{MPa}$ (corresponding to an applied strain of $\sim 0.31 \%$ in our UFG Ni specimens) and with the single-crystal elastic constants of Ni given in [46], Eq. (3) becomes
$W=\left(8.3607 \times 10^{5}+1.8768 \times 10^{5} \times \Gamma\right) \mathrm{J} / \mathrm{m}^{3}$
Based on Eq. (5), we plot the linear curve of $W$ versus $3 \Gamma$ in Fig. 5c. It is seen that among all the grain orientations along the loading direction, the [100] grain family has the smallest $W$, while the [111] grain family has the largest $W$. This grain orientation dependence can be directly correlated to the smallest and largest effective elastic constant of the [100] and [111] grain family along the loading direction, respectively [46]. According to Eq. (1), a GB will migrate favorably from the grain with lower $W$ towards
its neighboring grain with higher $W$, thereby reducing the total elastic strain energy of the polycrystalline aggregate. Hence, the growth of grains in the [100] family is most favorable energetically, which is consistent with the observed abnormal grain growth shown in Figs. 3 and 4. In addition, we have developed a phasefield model that accounts for the strain energy dominated driving force of grain growth and thus produces the direct simulation result of preferential growth of grains in the [100] family, which is consistent with the micromechanics model. This phase-field study will be reported in a follow-up paper.

The above micromechanics analysis is independent of grain size. One effect of having ultrafine grains with high yield strengths is their prevailing high stresses which raise strain energy densities (and accordingly strain energy density differences between neighboring grains) relative to coarse-grained counterparts, thereby increasing the thermodynamic driving force of grain growth to accumulate a sufficient amount of grain growth observable within a certain load cycles in laboratory experiment. In our theoretical analysis, a grain of certain orientation under consideration is assumed to embed in a homogenized medium of a polycrystalline matrix, and the effective stiffness of this grain is evaluated with respect to the surrounding homogenized matrix. This mean-field analysis can capture the primary effect of elastic anisotropy on the driving force of grain growth. However, direct elastic interactions between neighboring grains are not taken into account in the analysis. As a result, our mean-field solution could not cover cases where neighboring grains have relatively large variations in
stiffness, such that their driving forces for grain growth could deviate from the mean-field solution. Nonetheless, our analysis captures the predominant effect of elastic anisotropy on preferential growth of the [100] grain family.

As discussed above, the impact of elastic anisotropy on the abnormal growth of the [100] grain family can be effectively brought out in the high-cycle loading regime at room temperature, as indicated in Fig. 1. If either temperature or maximum applied strain (i.e., low-cycle loading or large monotonic loading) is increased, larger driving forces (due to higher GB energy and mobility, and/or higher plastic dissipation) will instead lead to normal grain growth. Hence, the elastic anisotropy regime illustrated in the mechanism map in Fig. 1 is likely to be confined to low strains and temperatures and therefore low grain growth rates that can only lead to substantial grain growth under large numbers of load cycles. Our MEMS microresonator-based setup facilitates tests in the highcycle fatigue regime (up to $10^{8}-10^{9}$ cycles) and thus allows much smaller average grain growth rates, down to $3 \times 10^{-5} \mathrm{~nm} /$ cycle, which is likely related to much lower plastic strain amplitudes in the low driving force regime. In this regard, the absence of grain growth at $0.15 \%$ can be interpreted as a threshold level in plastic strain amplitude below which the GB migration velocity is drastically reduced, despite having a thermodynamic driving force only slightly lower than that at $0.18 \%$ (for which grain growth occurred). The kinetics of GB migration under cyclic loading and the underlying mechanisms are still largely unexplored. A modification of the current experimental setup will be pursued to enable in situ SEM/EBSD cyclic testing and further investigate the kinetics of grain growth under cyclic loading. We note that similar abnormal grain growth associated with elastic anisotropy was not observed in recent cycle-induced grain growth studies with different fcc metals, initial grain sizes, and loading conditions [4,17-27]. Additional studies are therefore required to further understand the low driving force regime of abnormal grain growth illustrated in Fig. 1.

To summarize, this work demonstrates the occurrence of abnormal grain growth under cyclic deformation in the high-cycle fatigue regime. It provides a strong motivation for future investigation of abnormal grain growth behaviors dominated by the effect of elastic anisotropy (as illustrated in Fig. 1) in a variety of material systems by varying composition (e.g., from binary alloys to high-entropy alloys), lattice structure (e.g., from body-centered cubic to complex alloy structures), microstructural geometry (e.g., from bimodal to gradient distributions of grain size), thermomechanical loading (e.g., from liquid nitrogen to high temperatures), among others. Studies along these lines are essential to harnessing this unexpected phenomenon to tailor grain microstructures toward the development of novel high-performance materials.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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